

# Introduction to Graphing Rational Functions

$$\begin{aligned}x+4 &= 0 \\x &= -4\end{aligned}$$

Find any x-intercepts, y-intercepts, Vertical Asymptotes, Holes, and Horizontal Asymptotes

$$y = \frac{2x+3}{(x-2)}$$

H.A:  $y=2$

Holes: None

y-int:  $-1.5$

x-int:  $-1.5$

V.A:  $x=2$

H.A:  $y=0$

Holes: None

y-int:  $-.6$

x-int:  $3$

V.A:  $x=-5$   $x=-1$

$$\begin{aligned}x-3 &= 0 \\x &= 3 \\y &= \frac{x-3}{x^2+6x+5}\end{aligned}$$

$$x+5=0$$

$$x=-5$$

$$x+1=0$$

$$x=-1$$

H.A:  $y=1$

Holes:  $(-4, 1.3)$

y-int:  $2$

x-int:  $4$

V.A:  $x=2$

$$\boxed{\frac{x-4}{x-2}} = \frac{-8}{-6}$$

$$y = \frac{x-3}{(x+5)(x+1)} \quad y = \frac{\cancel{(x+4)}\cancel{(x-4)}}{\cancel{(x-2)}\cancel{(x+4)}} = \frac{x^2-16}{x^2+2x-8}$$

$$y = \frac{2x + 3}{(x - 2)}$$

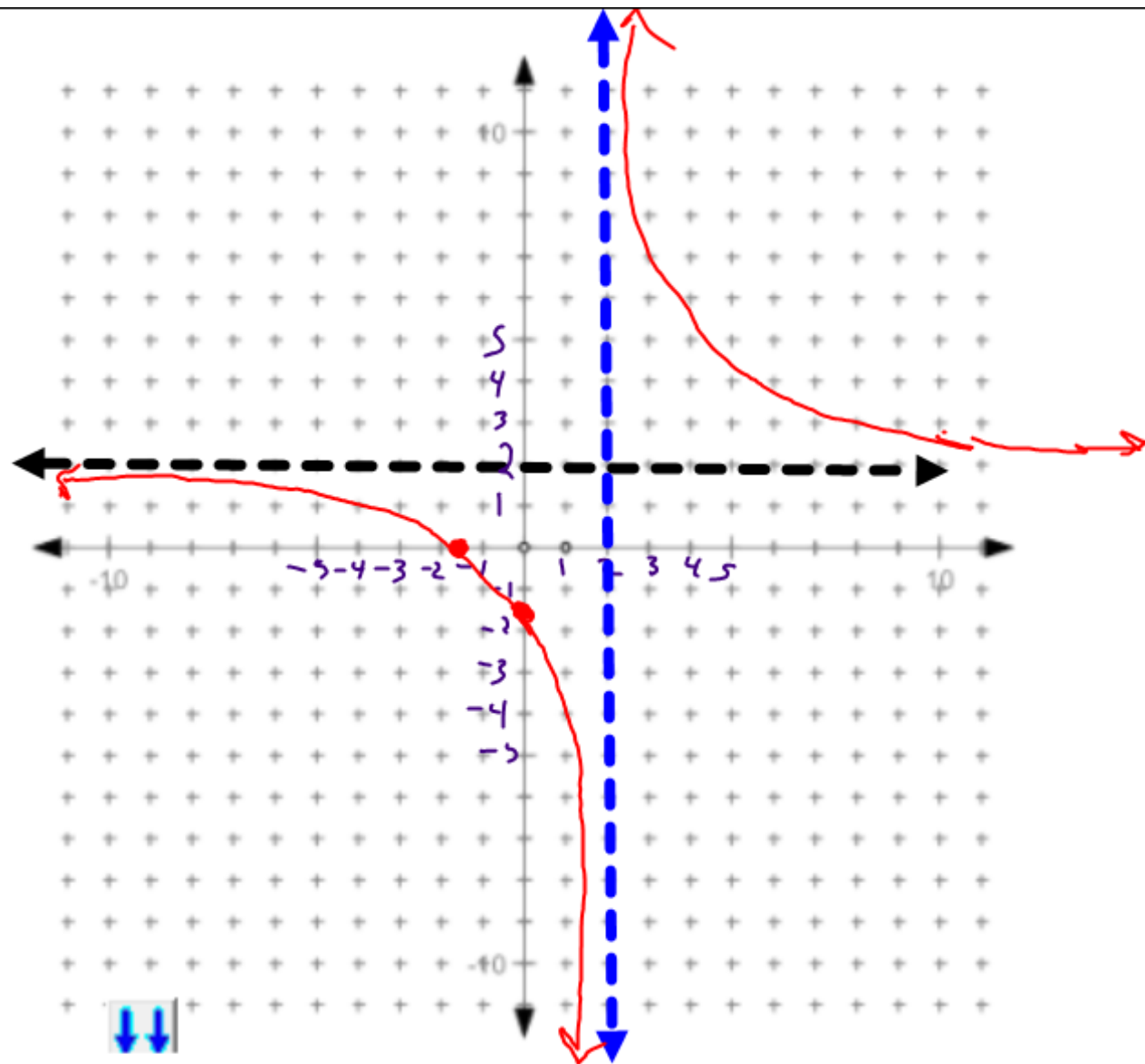
H.A:  $y = 2$

Holes: None

y-int:  $-1.5$

x-int:  $-1.5$

V.A:  $x = 2$



$$y = \frac{x-3}{x^2 + 6x + 5}$$

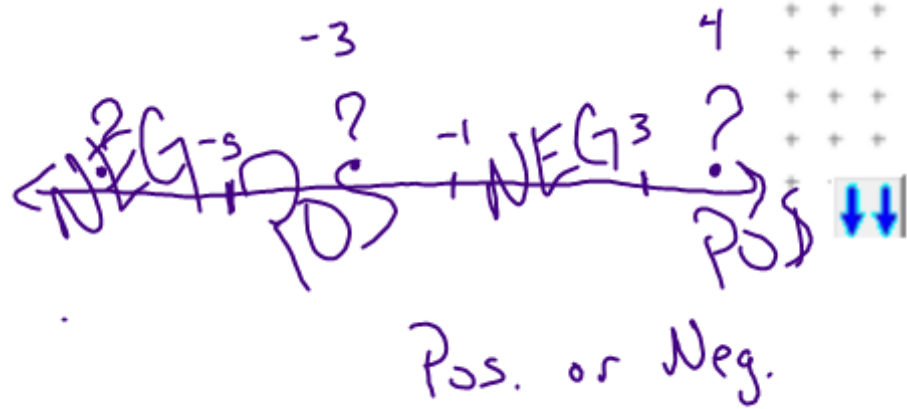
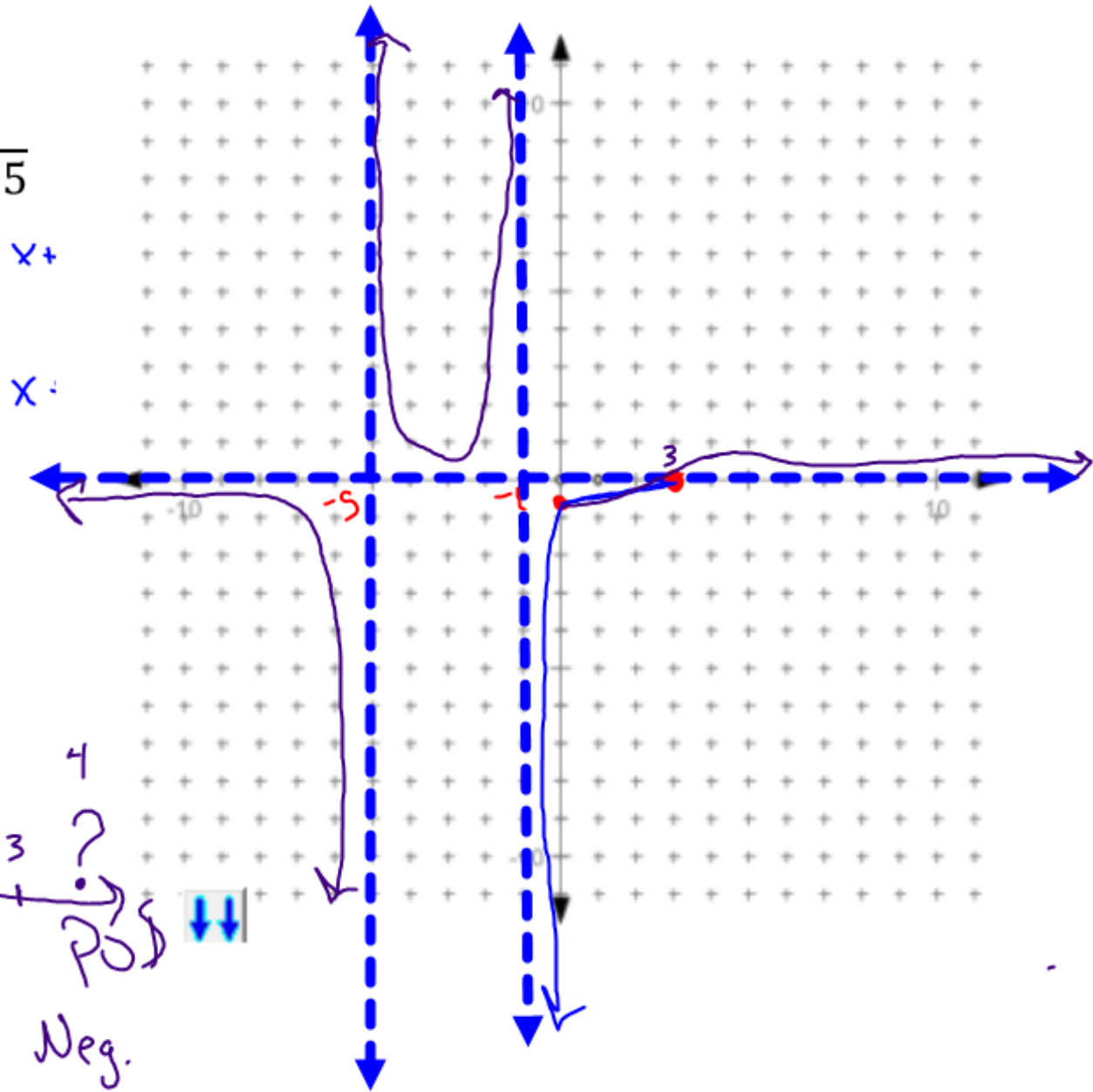
H.A:  $y=0$

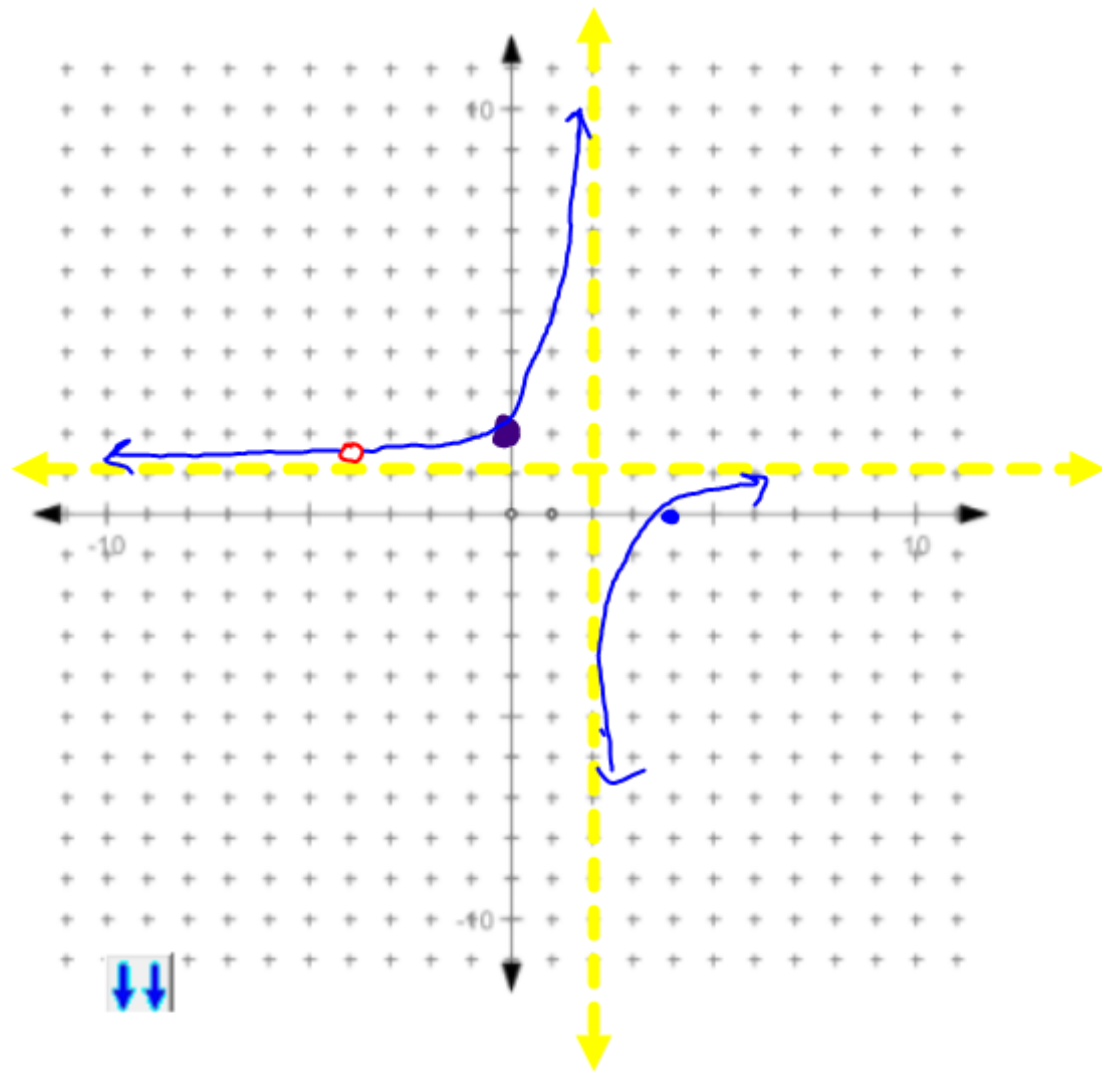
Holes: None

y-int:  $-0.6$

x-int:  $3$

V.A:  $x=-5, x=-1$





$$\frac{-3}{(x+1)} \left. \vphantom{\frac{-3}{(x+1)}} \right\} y = \frac{\cancel{(x-2)}\cancel{(x+4)}}{\cancel{x^2 - 16}} = \frac{-3}{x^2 + 2x - 8}$$

H.A:  $y = 1$

Holes:  $(-4, 1.3)$

y-int: 2

x-int: 4

V.A:  $x = 2$

$$\boxed{\frac{x-4}{x-2}} = \frac{-8}{-6}$$

# Graphing Rational Functions

Graphing Rational Functions:

- Find and graph the VA and HA
- Find and graph the  $x$  and  $y$  Intercepts and any holes (if any)
- Use a chart to evaluate additional points to show what the graph does on each section of graph (using your VA to split into sections)

# Parent Function:

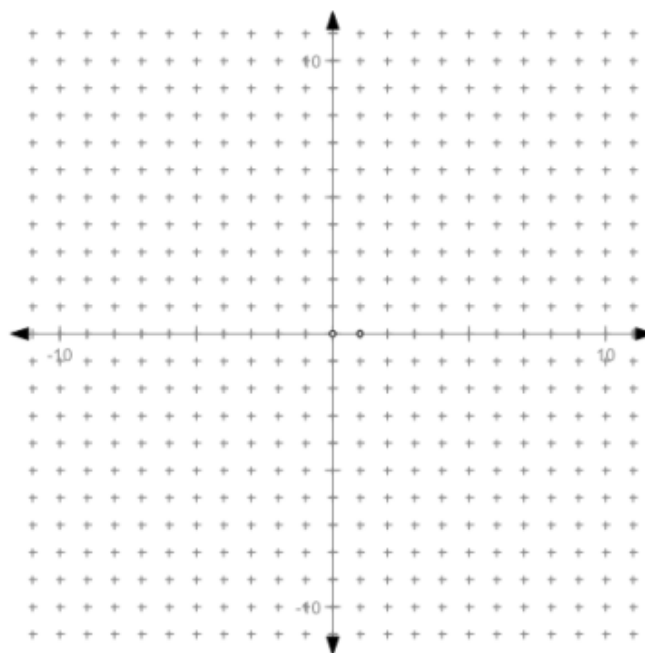
$$f(x) = \frac{1}{x}$$

VA:

HA:

Holes:

Intercepts:



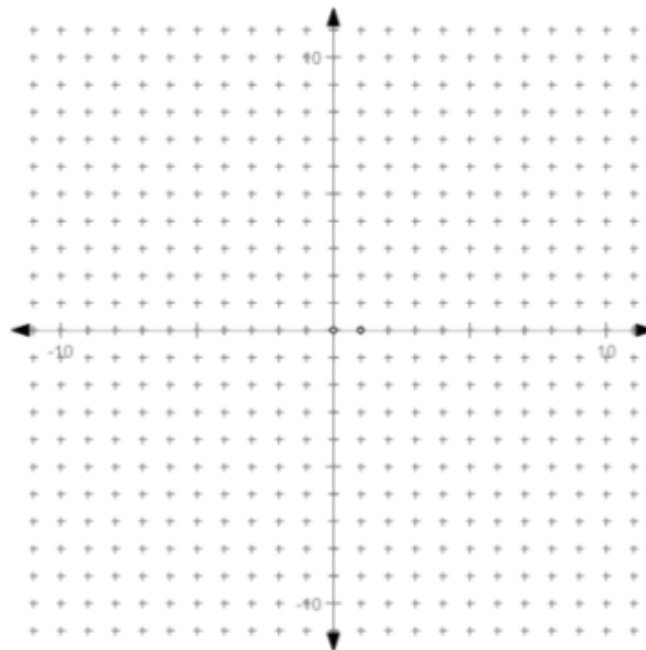
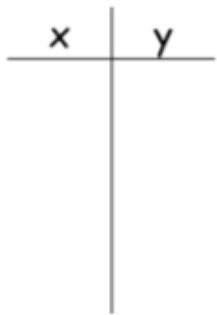
$$a) f(x) = \frac{2x-1}{x-3}$$

VA:

HA:

Holes:

Intercepts:



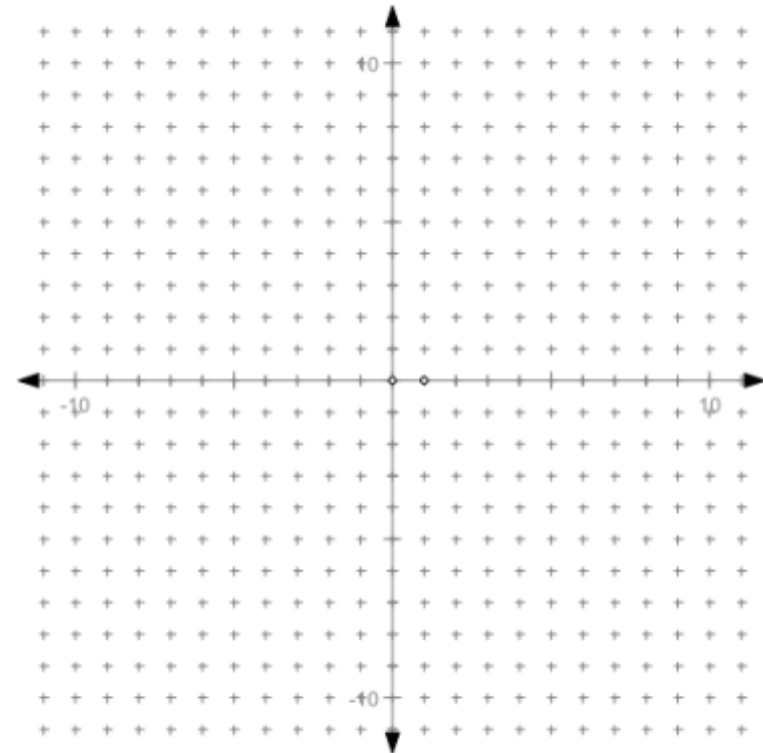
$$b) f(x) = \frac{2x^2 - 18}{x^2 - 4}$$

VA:

HA:

Holes:

Intercepts:





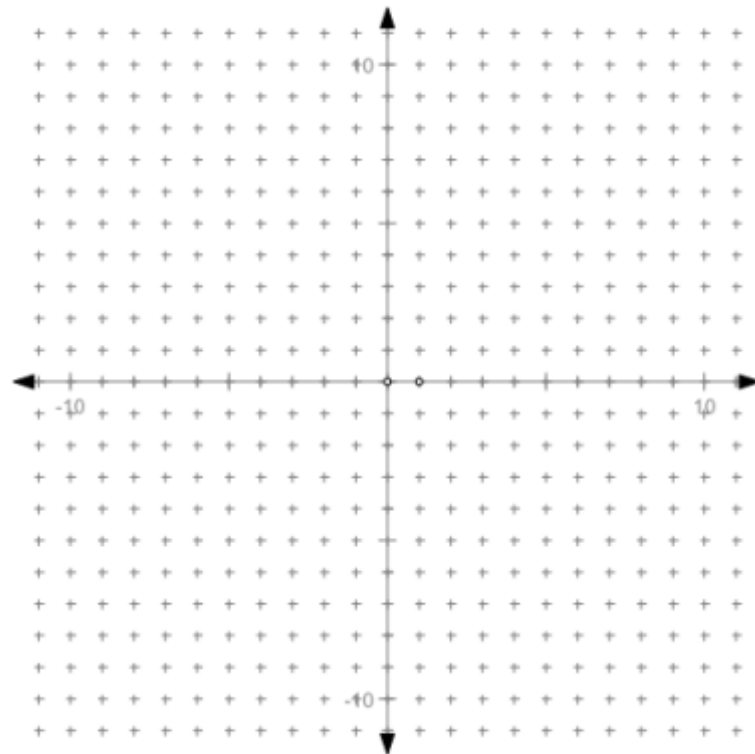
$$c) f(x) = \frac{2x-4}{x-1}$$

VA:

HA:

Holes:

Intercepts:



$$d) f(x) = \frac{\cancel{x+3}}{x^2-3x+2} x+3$$

$$\frac{x+3}{(x-2)(x-1)}$$

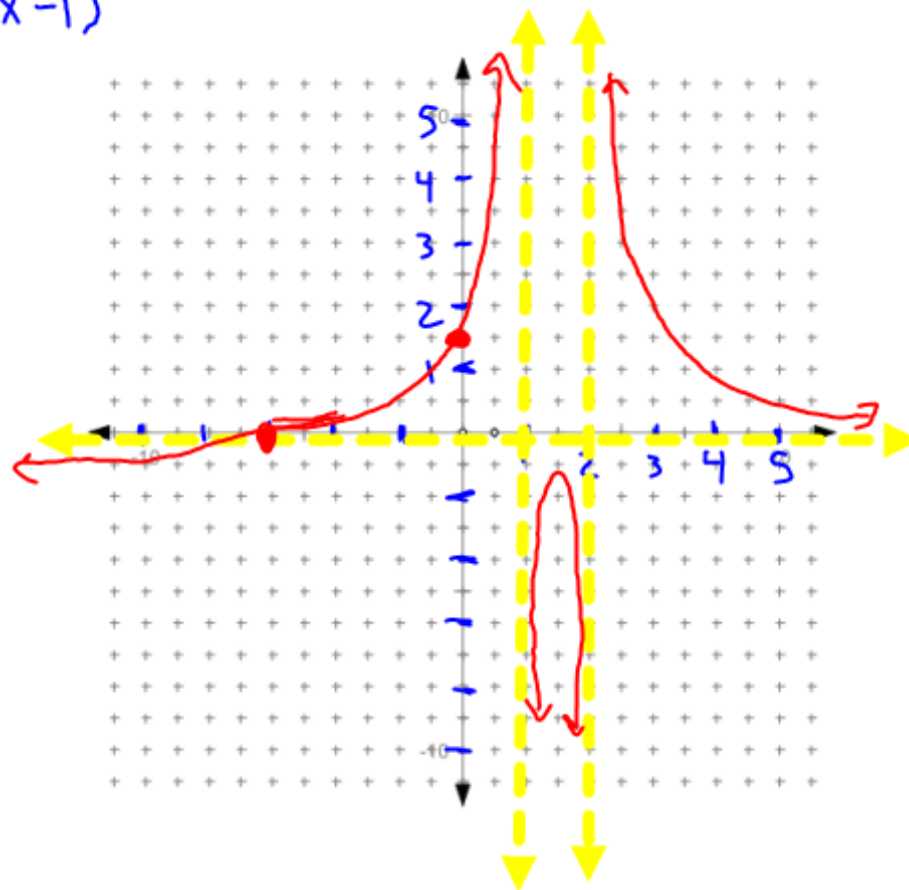
VA:  $x=2$   $x=1$

HA:  $y=0$

Holes: None

Intercepts:  $x$ -int:  $-3$

$y$ -int:  $1.5$



# Homework:

Graphing  
Rational  
Functions  
Worksheet #1