

E.Q.: How do we create and solve linear equations in two variables?

Standard: MGSE9-12.A.CED.2

Create linear equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

(The phrase “in two or more variables” refers to formulas like the compound interest formula, in which $A = P(1 + r/n)^t$ has multiple variables.)

Vocabulary:

linear equation:

- an algebraic equation in which each term is either a constant or the product of a constant and (the first power of) a single variable. 4 or -2
 $4x$ or $-2x$ or $\frac{3}{4}x$
- Linear equations can have one or more variables.

Slope - intercept form

$$y = \underline{m} \cdot x + \underline{b} \text{ (y-int)}$$

$$y = 4x - 2$$

$$y = 4x$$

$$y = x - 3$$

$$y = 5$$

independent variable: (x)

- It is a variable that stands alone and isn't changed by the other variables you are trying to measure.
- For example, someone's age might be an independent variable.

$$y = mx + b$$

Handwritten annotations for the equation $y = mx + b$:

- An arrow points from the word "slope" to the coefficient m .
- An arrow points from the text "y-int." to the constant term b .
- An arrow points from the text "independent variable" to the variable x .

dependent variable: (y)

- A dependent variable is what you measure in the experiment and what is affected during the experiment.
- The dependent variable responds to the independent variable.
- It is called dependent because it "depends" on the independent variable.

(m)

Slope and Rate of Change:

- The word slope (gradient, incline, pitch) is used to describe the measurement of the steepness of a straight line.
- The higher the slope, the steeper the line.
- The slope of a line is a rate of change.

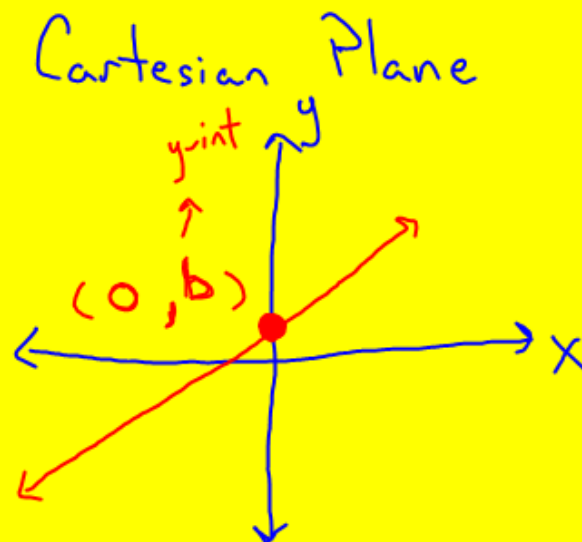
$$m = \frac{\text{rise}}{\text{run}} = \frac{\text{change in } y}{\text{change in } x} = \frac{\Delta y}{\Delta x}$$

delta

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

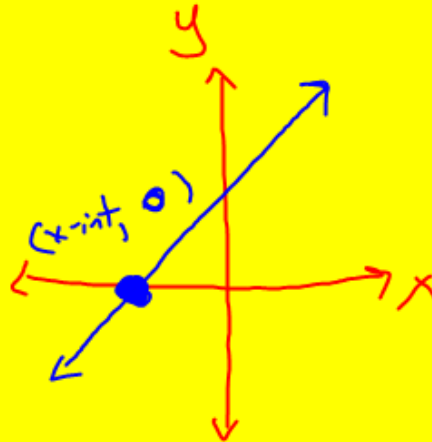
y-intercept:

- is a point where the graph of an equation intersects with the y-axis of the coordinate system.
- these points satisfy $x = 0$.



x-intercept:

- is a point where the graph of a function or relation intersects with the x-axis.
- these points satisfy $y=0$.



Multiple Representations of a Linear Relationship

$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{2}{1}$$

Equation

$$y = mx + b$$

$$y = \underline{2}x + \underline{1}$$

slope - intercept

$$y - \underline{3} = \underline{2}(x - \underline{1})$$

point-slope form

$$y - y_1 = m(x - x_1)$$

$$y - 7 = 2(x - 3)$$

$$y + 3 = 2(x + 2)$$

Table

X	Y
-2	-3
-1	-1
0	1
1	3
2	5
3	7

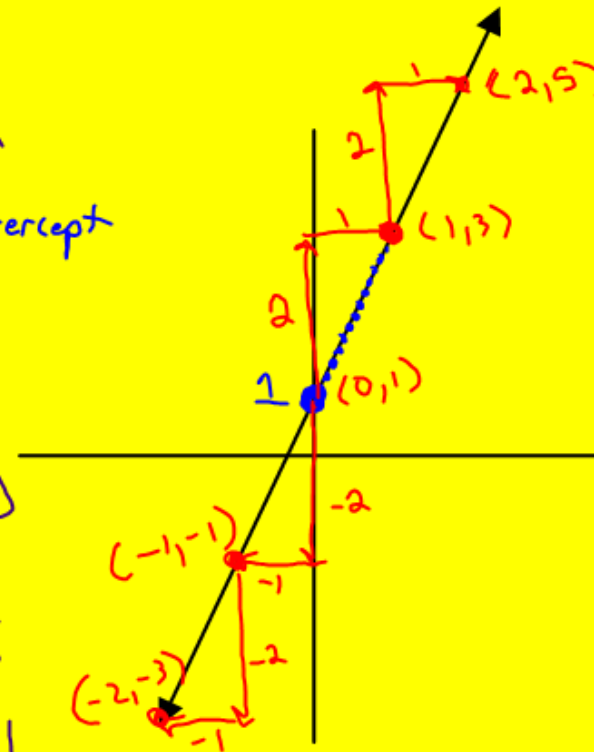
\leftarrow +2
 \leftarrow +3
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 \leftarrow +2
 \leftarrow +2
 \leftarrow +2
 y-intercept

$$y - 3 = 2(x - 1)$$

$$y - 3 = 2x - 2$$

$$y = \underline{\underline{2x + 1}}$$

Graph



Given the following equation, $y = 4x + 3$,
create a table of values that is representative
of that equation.

$$y = 4x + 3$$

X	y
-2	$4(-2) + 3 = -5$
-1	$4(-1) + 3 = -1$
0	$4(0) + 3 = 3$
1	$4(1) + 3 = 7$
2	$4(2) + 3 = 11$
3	$4(3) + 3 = 15$

$\left. \begin{array}{l} \leftarrow +4 \\ \leftarrow +4 \\ \leftarrow +4 \end{array} \right\} +4$

$\left. \begin{array}{l} \leftarrow +4 \\ \leftarrow +4 \end{array} \right\} +4$

$\left. \begin{array}{l} \leftarrow +4 \\ \leftarrow +4 \end{array} \right\} +4$

Given the following equation, $y = -2x + 5$, create a table of values that is representative of that equation.

X	y
-2	9
-1	7
0	5
1	3
2	1
3	-1

$$-2(-2) + 5$$

y-int

-2

-2

-2

Given the following table,
is this table representative of a linear relationship?

If so, what is the equation?

x	y
-2	-15
-1	-10
0	-5
1	0
2	5
3	10

$$y = mx + b$$

$$y = 5x - 5$$

$$-5 = 5(0) - 5$$

$$-5 = 0 - 5$$

$$-5 = -5 \checkmark$$

$$5 = 5(2) - 5$$

$$= 10 - 5$$

$$= 5 \checkmark$$

Given the following table,
is this table representative of a linear relationship?

If so, what is the equation?

x	y
-5	-15
0	-10
5	-5
10	0
15	5
20	10

Handwritten annotations: On the left side of the table, there are five arrows pointing left, each labeled '+5', indicating a constant increase in x. On the right side, there are five arrows pointing right, each labeled '+5', indicating a constant increase in y. A circled '+5' is written to the right of the table.

~~$$y = 5x - 10$$~~

$$-10 = 5(0) - 10$$

$$-10 = 0 - 10$$

$$-10 = -10$$

$$0 = 5(10) - 10$$

$$= 50 - 10$$

$$0 = 40 \quad \times$$

$$y = x - 10$$

$$\text{Slope} = \frac{\text{rise}}{\text{run}} = \frac{\Delta y}{\Delta x} = \frac{5}{5} = 1$$

Given the following table,
is this table representative of a linear relationship?

If so, what is the equation?

x	y
-2	-15
0	-10
3	-5
10	0
15	5
50	10

2 < } 5
3 < } 5

$$m = \frac{5}{2} = 2.5$$

$$m = \frac{5}{3} = 1.\bar{6}$$

~~$$y = mx + b$$~~

~~$$y = mx - 10$$~~

No
There is no constant rate of change!

Ex. The data below represent the value of a car as it depreciates over a period of 5 years.

Years	0	1	2	3	4	5
Value	15000	12400	9800	7200	4600	2000

-2600

independent variable = # of years = x

dependent variable = value of car = y

$$\frac{-2600}{1}$$



$$m = -2600$$

Calculate and interpret the **slope**.

For each additional year, the car's value decreased by 2600.

Ex. The data below represent the value of a car as it depreciates over a period of 5 years.

Years	0	1	2	3	4	5
Value	15000	12400	9800	7200	4600	2000

State and interpret the y -intercept.

15,000

When the car is new, at $time = \underline{0 \text{ years}}$, the car is worth $\underline{\$ 15,000}$.

Ex. The data below represent the value of a car as it depreciates over a period of 5 years.

Years	0	1	2	3	4	5
Value	15000	12400	9800	7200	4600	2000

Write an equation that models this relationship:

$$y = \underline{m}x + \underline{b}$$

$$y = -2600x + 15000$$

Use your model to determine
the value of the car at 3.5 years.

"y" $y = -2600x + 15000$

$$y = -2600(3.5) + 15000$$

$$y = \cancel{\$8500} \quad \$5900$$

Use your model to determine when^x
the car will be worth \$700^y?

$$y = -2600x + 15000$$

$$\begin{array}{r} 700 = -2600x + 15000 \\ -15000 \quad \quad \quad -15000 \\ \hline \end{array}$$

$$\begin{array}{r} -14300 = -2600x \\ -2600 \quad \quad \quad -2600 \\ \hline \end{array}$$

$$x = 5.5 \text{ years}$$

The table below shows the depth in meters of a scuba diver after a certain amount of time under water.

Position of Scuba Diver	
Time (s)	Depth (m)
x	y
0	-24
3	-18
6	-12
9	-6
12	0

independent variable =

dependent variable =

Find the average rate of change for this relationship. Interpret this value.

average rate of change = _____

For each additional _____ that elapses, the diver has risen _____ meters under the surface of the water.

State and interpret the y-intercept. y-intercept = _____

At time = _____, the scuba diver is _____ meters under the surface of the water.

Position of Scuba Diver	
Time (s)	Depth (m)
x	y
0	-24
3	-18
6	-12
9	-6
12	0

Write an equation that models this relationship:

$$y = mx + b$$

Position of Scuba Diver	
Time (s)	Depth (m)
x	y
0	-24
3	-18
6	-12
9	-6
12	0

Use your model to determine the diver's depth at 5 seconds. _____

Use your model to predict how many seconds it takes the diver reach 9 meters below the surface. _____

Homework #4: Two Variable Equations