

Warmup: Solve by completing the square

$$3x^2 - 12x + 6 = 0$$

$$\begin{array}{c} 9 \\ 3 \quad 3 \\ \times \\ 6 \end{array}$$

$$x^2 + 6x - 7 = 0$$

$$+ 7 \quad + 7$$

$$x^2 + 6x + \frac{9}{9} = 7 + 9$$

$$\sqrt{(x+3)^2} = \sqrt{16}$$

$$\begin{array}{c} x+3 \\ -3 \end{array} = \begin{array}{c} \pm 4 \\ -3 \end{array}$$

$$x = -3 \pm 4$$

$$-3 + 4 = (1)$$

$$-3 - 4 = (-7)$$

$$\frac{6}{2} = \boxed{3}$$

$$3^2 = 9$$

$$\begin{array}{c} 4 \\ -2 \quad -2 \\ -4 \end{array}$$

$$3x^2 - 12x + 6 = 0$$

$$-6 \quad -6$$

$$3x^2 - 12x = -6$$

$$3(x^2 - 4x + \underline{4}) = -6 + \underline{12}$$

$$\frac{3(x-2)^2}{3} = \frac{6}{3}$$

$$\sqrt{(x-2)^2} = \sqrt{2}$$

$$x-2 = \pm\sqrt{2}$$

$$x = 2 \pm \sqrt{2}$$

$$\frac{-4}{2} = \underline{-2}$$

$$(-2)^2 = 4$$

1) $v^2 + 12v - 15 = 0$

$$v^2 + 12v + \underline{36} = 15 + \underline{36}$$

$$\frac{12}{2} = 6$$

$$6^2 = 36$$

$$(v+6)^2 = 51$$

$$v+6 = \pm \sqrt{51}$$

$$v = -6 \pm \sqrt{51}$$

2) $r^2 - 20r + 33 = 0$

$$r^2 - 20r + \underline{100} = -33 + \underline{100}$$

$$\frac{-20}{2} = -10$$

$$(r-10)^2 = 67$$

$$(-10)^2 = 100$$

$$r-10 = \pm \sqrt{67}$$

$$r = 10 \pm \sqrt{67}$$

3) $r^2 + 20r + 99 = 0$

$$r^2 + 20r + \underline{100} = -99 + \underline{100}$$

$$\frac{20}{2} = 10$$

$$(r+10)^2 = 1$$

$$r+10 = \pm 1$$

$$r = -10 \pm 1$$

$$r = -9 \text{ or } -11$$

4) $v^2 - 6v + 5 = 0$

$$v^2 - 6v + \underline{9} = -5 + \underline{9}$$

$$\frac{-6}{2} = -3$$

$$(v-3)^2 = 4$$

$$(-3)^2 = 9$$

$$v-3 = \pm 2$$

$$v = 3 \pm 2$$

$$v = 5 \text{ or } 1$$

$$5) 6r^2 - 12r - 79 = 0$$

$$\underline{6r^2} - \underline{12r} = 79$$

$$6(\underline{1r^2} - \underline{2r} + \underline{1}) = 79 + \underline{6}$$

$$\frac{-2}{2} = -1$$

$$6(r-1)^2 = 85$$

$$(-1)^2 = 1$$

$$(r-1)^2 = \frac{85}{6}$$

$$r-1 = \pm \sqrt{\frac{85}{6}}$$

$$r = 1 \pm \sqrt{\frac{85}{6}}$$

$$6) 5k^2 - 10k - 75 = 0$$

$$5k^2 - 10k = 75$$

$$5(k^2 - 2k + \underline{1}) = 75 + \underline{5}$$

$$\frac{-2}{2} = -1$$

$$5(k-1)^2 = 80$$

$$(-1)^2 = 1$$

$$(k-1)^2 = 16$$

$$k-1 = \pm 4$$

$$k = 1 \pm 4$$

$$k = 5 \text{ or } -3$$

$$7) 10p^2 - 20p - 30 = 0$$

$$10p^2 - 20p = 30$$

$$10(p^2 - 2p + \underline{1}) = 30 + \underline{10}$$

$$\frac{-2}{2} = -1$$

$$10(p-1)^2 = 40$$

$$(-1)^2 = 1$$

$$(p-1)^2 = 4$$

$$p-1 = \pm 2$$

$$p = 1 \pm 2 \quad p = 3 \text{ or } -1$$

$$8) 3a^2 + 6a - 42 = 0$$

$$3a^2 + 6a = 42$$

$$3(a^2 + 2a + \underline{\quad}) = 42 + \underline{\quad}$$

$$\frac{2}{2} = 1$$

$$3(a^2 + 2a + 1) = 42 + 3$$

$$1^2 = 1$$

$$3(a+1)^2 = 45$$

$$(a+1)^2 = 15$$

$$a+1 = \pm \sqrt{15}$$

$$a = -1 \pm \sqrt{15}$$

$$9) b^2 = 70 - 4b$$

$$b^2 + 4b + \underline{4} = 70 + \underline{4}$$

$$\frac{4}{2} = 2$$

$$(b+2)^2 = 74$$

$$\frac{2}{2} = 1$$

$$b+2 = \pm \sqrt{74}$$

$$1^2 = 1$$

$$b = -2 \pm \sqrt{74}$$

$$10) x^2 = -2x + 63$$

$$x^2 + 2x + \underline{1} = 63 + \underline{1}$$

$$(x+1)^2 = 64$$

$$x+1 = \pm 8$$

$$x = -1 \pm 8$$

$$x = 7 \text{ or } -9$$

$$11) 7v^2 - 21 = -14v$$

$$7v^2 + 14v = 21$$

$$7(v^2 + 2v + \underline{1}) = 21 + \underline{7}$$

$$\frac{2}{2} = 1$$

$$7(v+1)^2 = 28$$

$$1^2 = 1$$

$$(v+1)^2 = 4$$

$$v+1 = \pm 2$$

$$v = -1 \pm 2$$

$$v = 1 \text{ or } -3$$

$$12) 5n^2 + 20n = 66$$

$$5(n^2 + 4n + \underline{4}) = 66 + \underline{20}$$

$$\frac{4}{2} = 2$$

$$5(n+2)^2 = 86$$

$$2^2 = 4$$

$$(n+2)^2 = \frac{86}{5}$$

$$n+2 = \pm \sqrt{\frac{86}{5}}$$

$$n = -2 \pm \sqrt{\frac{86}{5}}$$

E.Q.:

How do we solve quadratic equations
using the quadratic formula?

SHORTCUT To Completing The Square?

The Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

This formula works for all standard form quadratic equations.

It is directly derived by completing the square on the standard form of a quadratic equation:

$$ax^2 + bx + c = 0$$

We have studied several different ways to solve quadratic equations (factoring and taking square roots). These methods may not work in certain instances. The **Quadratic Formula** is a method of solving quadratics that **works for every quadratic equation.**

☆ -In order to set up quadratic formula, we need our quadratic equation written in standard form:

$$ax^2 + bx + c = 0$$

☆ -Once the quadratic is in standard form, we plug **the Coefficients** a, b, and c into the quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Solve using the quadratic formula:

$$x^2 + 6x + 5 = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-6 \pm \sqrt{(6)^2 - 4(1)(5)}}{2(1)}$$

$$a = 1$$

$$b = 6$$

$$c = 5$$

$$x = \frac{-6 \pm \sqrt{16}}{2}$$

$$x = \frac{-6 \pm 4}{2}$$

$$x = \frac{-6+4}{2} = \frac{-2}{2} = \textcircled{-1}$$

$$x = \frac{-6-4}{2} = \frac{-10}{2} = \textcircled{-5}$$

EXAMPLES Set up the quadratic formula for each of the following quadratic equations.

$$6x^2 - 45 = 3x$$

$-3x$ $-3x$

$$6x^2 - 3x - 45 = 0$$

$$X = \frac{3 \pm \sqrt{(-3)^2 - 4(6)(-45)}}{2(6)}$$

$$a = 6$$

$$b = -3$$

$$c = -45$$

$$X = \frac{3 \pm \sqrt{1089}}{12}$$

$$X = \frac{3 \pm 33}{12}$$

$$X = \frac{3 + 33}{12} = \frac{36}{12} = 3$$

$$X = \frac{3 - 33}{12} = \frac{-30}{12} = -\frac{5}{2}$$

$$4x^2 = -9 - 9x$$

$\swarrow +9 \quad \swarrow +9x$

$$4x^2 + 9x + 9 = 0$$

$$a = 4$$

$$b = 9$$

$$c = 9$$

$$\frac{-9 \pm \sqrt{(9)^2 - 4(4)(9)}}{2(4)}$$

$$\frac{-9 \pm \sqrt{-63}}{8}$$

No real roots
or
No real solutions

$$x^2 + 6x + 6 = 0$$

$$a = 1$$

$$b = 6$$

$$c = 6$$

$$x = \frac{-6 \pm \sqrt{(6)^2 - 4(1)(6)}}{2(1)}$$

$$x = \frac{-6 \pm \sqrt{12}}{2}$$

$$x = \frac{-6 \pm 2\sqrt{3}}{2}$$

$$x = \frac{-6 + 2\sqrt{3}}{2} \quad \text{or} \quad \frac{-6 - 2\sqrt{3}}{2}$$

$$x = \sqrt{3} - 3 \quad \text{or} \quad -\sqrt{3} - 3$$

$$(-3 \pm \sqrt{3})$$

$$5x^2 = 80$$

$$5x^2 - 80 = 0$$

$$a = 5$$

$$b = 0$$

$$c = -80$$

$$x = \frac{0 \pm \sqrt{0^2 - 4(5)(-80)}}{2(5)}$$

$$x = \frac{\pm \sqrt{1600}}{10}$$

$$x = \frac{\pm 40}{10}$$

$$x = -4 \text{ or } +4$$

HW #7:
Solving Quadratic Equations
Using the Quadratic Formula